MATH 2260 (Ordinary Differential Equations I) — Fall 2014 Midterm Exam #1 Review problems

Section 1.2: #1, 4, 6 Section 1.3: #1, 5, 9 Section 2.1: #3, 4, 9, 18, 20, 32, 40 Section 2.2: #4, 6, 12, 19 Section 2.3: #6, 8, 10 Section 2.4: #4, 10, 11, 16, 26, 28, 48 Section 2.5: #2, 4, 6, 12, 14, 20, 22 Section 2.6: #4, 6, 14, 20

MATH 2260 (Ordinary Differential Equations I) — Fall 2014 Practice Midterm Exam #1

- 1. (20 points) Solve $2x\frac{dy}{dx} + \cos^2(y)\ln(x) = 0.$
- 2. (20 points) Solve $x^2 \frac{dy}{dx} 3x^2y = x^3$.
- 3. (10 points) Show that $(y x)\frac{dy}{dx} 7y = xe^{y/x}$ is a homogeneous nonlinear equation.
- 4. (20 points) Solve $\frac{dy}{dx} \frac{1}{7}y = x/y^6$.
- 5. (10 points) Is $y(x) = xe^{2/x}$ a solution of $x^3y'' + 2xy' 2y = 0$?
- 6. (20 points) Consider $(2x^2 + y)dx + (x^2y x)dy = 0$
 - (a) Show that the equation is not exact.
 - (b) Find an integrating factor to make it exact.
 - (c) Find an implicit definition of the solution y(x).