## MEMORIAL UNIVERSITY OF NEWFOUNDLAND DEPARTMENT OF MATHEMATICS AND STATISTICS

Section 2.3	Math 2000 Worksheet	Fall 2018

## For practice only. Not to be submitted.

- 1. Find all the first-order partial derivatives for each of the following functions.
  - (a)  $z = \sin(x) \cos(y)$ (b)  $f(x, y) = y^{x}$ (c)  $f(s, t) = \arctan\left(\frac{s^{2}}{t^{2}}\right)$ (d)  $z = \cos(3x - 5y)$  at the point  $\left(\frac{\pi}{6}, \frac{\pi}{15}, \frac{\sqrt{2}}{2}\right)$ (e)  $w = xy^{2}z^{3}$ (f)  $f(x, y, z) = \frac{6xy}{\sqrt{25 - z^{2}}}$  at the point (1, 2, 4, 4).
- 2. Find all the second-order partial derivatives of  $f(x, y) = xye^{y}$ . Does Clairault's Theorem hold for this function?
- 3. Determine which of the following functions are solutions of Laplace's equation.
  - (a)  $f(x, y) = x^2 y^2$ (b)  $f(x, y) = x^2 + y^2$ (c)  $f(x, y) = \ln[(x^2 + y^2)^2]$ (d)  $f(x, y) = e^{-x} \cos(y) - e^{-y} \cos(x)$
- 4. Show that  $u = \sin(kx)\sin(\alpha kt)$  is a solution of the wave equation

$$\frac{\partial^2 u}{\partial t^2} = \alpha^2 \frac{\partial^2 u}{\partial x^2},$$

where  $\alpha$  and k are constants.

5. Show that  $f(x,y) = xe^y + ye^x$  is a solution of the partial differential equation

$$f_{xxx}(x,y) + f_{yyy}(x,y) = xf_{xyy}(x,y) + yf_{xxy}(x,y).$$