MEMORIAL UNIVERSITY OF NEWFOUNDLAND DEPARTMENT OF MATHEMATICS AND STATISTICS

| Section 5.1 | Math 1090 Worksheet | Fall 2009 |
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For practise only. Not to be submitted.

- 1. Use long division to find the quotient Q(x) and the remainder R(x) when the polynomial $P(x) = 3x^4 4x^3 + 2x^2 + 10x 2$ is divided by
 - (a) $D(x) = x^2 2x + 3$
 - (b) D(x) = x + 1
- 2. Use synthetic division to find the quotient Q(x) and the remainder R(x) when
 - (a) $2x^3 + 3x^2 x + 5$ is divided by x + 3
 - (b) $2x^4 11x^2 + 8x + 3$ is divided by x 2
- 3. Find all roots (zeros) of each of the following polynomials.

(a)
$$P(x) = x^4 + 5x^3 - 3x^2 - 17x - 10$$

- (b) $P(x) = 6x^3 11x^2 4x + 4$
- (c) $P(x) = 2x^4 5x^3 4x^2 + 23x 10$
- (d) $P(x) = 2x^5 7x^4 + 18x^2 8x 8$
- (e) $P(x) = 9x^4 6x^3 + 19x^2 12x + 2$
- (f) $P(x) = x^4 2x^3 17x^2 + 30x + 8$
- 4. Factor each of the following polynomials completely into linear factors.
 - (a) $P(x) = 16x^4 64x^3 + 63x^2 + 4x 4$ (b) $P(x) = 2x^4 + 5x^3 - 11x^2 - 20x + 12$
 - (c) $P(x) = 3x^4 + 5x^3 + 10x^2 + 20x 8$
 - (d) $P(x) = 4x^5 11x^3 x^2 + 6x + 2$
- 5. Find all solutions (real and imaginary) of each of the following equations.

(a)
$$2x^4 + 3x^3 - 3x^2 - 7x - 3 = 0$$

(b) $8x^5 + 12x^4 + 14x^3 + 13x^2 + 6x + 1 = 0$

(c)
$$x^3 + x - 10 = 0$$

- 6. (a) Find a polynomial of lowest possible degree that has 2 as a root of multiplicity 3, and -1 as a root of multiplicity 1.
 - (b) Find a polynomial with real coefficients that has 3 and -1 + i as roots.
 - (c) Find a polynomial with real coefficients that has -4 and $3-2\sqrt{2}$ as roots, and for which P(0) = -8.