MEMORIAL UNIVERSITY OF NEWFOUNDLAND DEPARTMENT OF MATHEMATICS AND STATISTICS

Section 2.2

Math 1001 Worksheet

WINTER 2025

For practice only. Not to be submitted.

1. Express each of the following as a definite integral over the indicated interval [a, b], where x_i^* is the sample point on the *i*th subinterval.

(a)
$$\lim_{n \to \infty} \sum_{i=1}^{n} \frac{2}{(x_{i}^{*} - 4)^{2}} \Delta x_{i}$$
 over [6, 8]
(b) $\lim_{n \to \infty} \sum_{i=1}^{n} \cos^{3}(5x_{i}^{*}) \Delta x_{i}$ over $\left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$

2. Use the limit of a Riemann sum to compute each of the following. (In each case, use a regular partition and let the sample point be the right endpoint of the *i*th subinterval.) Does the definite integral represent the area under the curve in each case?

(a)
$$\int_{0}^{2} \frac{x^{3}}{4} dx$$

(b) $\int_{2}^{3} (2 - 7x) dx$