MEMORIAL UNIVERSITY OF NEWFOUNDLAND DEPARTMENT OF MATHEMATICS AND STATISTICS

Assignment 5

MATHEMATICS 1001

WINTER 2024

Due: Monday, March 4th, 2024 at 11:59pm. See the Gradescope Handout for submission information.

Note: You should complete the WebAssign problem sets "The Fundamental Theorem of Calculus I", "The Fundamental Theorem of Calculus II", and "Definite Integrals by u-Substitution", as well as Worksheet 2.3, before you work on this assignment.

1. Use the First Fundamental Theorem of Calculus to find f'(x), given

$$f(x) = \int_x^{x^2} \csc(t^3) \, dt.$$

2. Use the Second Fundamental Theorem of Calculus to evaluate each of the following definite integrals.

(a)
$$\int_{1}^{3} x \ln(x) dx$$

(b) $\int_{0}^{\frac{\pi}{6}} \tan^{5}(x) \sec^{2}(x) dx$
(c) $\int_{-5}^{4} |x^{2} - 9| dx$

3. Find the area of the region which lies under the curve $f(x) = x^3 - 2x + 4$, above the x-axis, and between the y-axis and the line x = 2.