MEMORIAL UNIVERSITY OF NEWFOUNDLAND

DEPARTMENT OF MATHEMATICS AND STATISTICS

Section 1.3

Math 1000 Worksheet

Fall 2023

For practice only. Not to be submitted.

1. Given that $\lim_{x\to p} f(x) = -5$ and $\lim_{x\to p} g(x) = 4$, find each of the following.

(a)
$$\lim_{x \to p} [f(x) - g(x)]$$
(c)
$$\lim_{x \to p} \frac{f(x)}{g(x)}$$

(b)
$$\lim_{x \to \infty} [g(x) - 2f(x)]$$

(c)
$$\lim_{x \to p} \frac{f(x)}{g(x)}$$

(b)
$$\lim_{x \to p} [g(x) - 2f(x)]$$
(d)
$$\lim_{x \to p} f(x) \sqrt{g(x)}$$

2. Evaluate each of the following limits.

(a)
$$\lim_{x \to 5} (x^2 - 9x + 3)$$

(b)
$$\lim_{x \to -3} \frac{\sqrt{1-x}}{x}$$

(c)
$$\lim_{h \to 0} \frac{\cos(h)}{2^h}$$

(d)
$$\lim_{x\to 2} \frac{|x-2|}{x-2}$$

3. Given

$$f(x) = \begin{cases} \cos(x) & \text{for } x \le 0\\ 1 - 4x & \text{for } 0 < x \le 3\\ \frac{9}{x} & \text{for } x > 3 \end{cases}$$

determine each of the following limits, or explain why the limit does not exist.

(a)
$$\lim_{x \to -\frac{\pi}{6}} f(x)$$

(b)
$$\lim_{x \to 0} f(x)$$

(c)
$$\lim_{x \to 3} f(x)$$

4. Find all values of k for which $\lim_{x\to -2} f(x)$ exists, given

$$f(x) = \begin{cases} k^2 x, & \text{for } x < -2\\ k - 6, & \text{for } x = -2\\ 4k - x, & \text{for } x > -2 \end{cases}$$