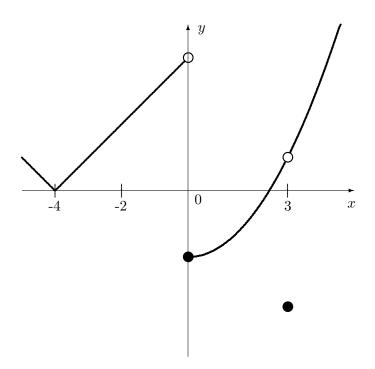
MEMORIAL UNIVERSITY OF NEWFOUNDLAND DEPARTMENT OF MATHEMATICS AND STATISTICS

TEST 2 MATHEMATICS 1000-002 OCTOBER 25TH, 2023 Name MUN Number

[12] 1. Use the graph of y = f(x) below to determine each of the following. When asked to classify a discontinuity, you should indicate whether it is removable or non-removable.



- (a) Is f(x) continuous at x = -4? If not, classify the discontinuity.
- (b) Is f(x) differentiable at x = -4? If not, briefly explain why.
- (c) Is f(x) continuous at x = 0? If not, classify the discontinuity.
- (d) Is f(x) differentiable at x = 0? If not, briefly explain why.
- (e) Is f(x) continuous at x = 1? If not, classify the discontinuity.
- (f) Is f(x) differentiable at x = 1? If not, briefly explain why.
- (g) Is f(x) continuous at x = 3? If not, classify the discontinuity.
- (h) Is f(x) differentiable at x = 3? If not, briefly explain why.

[5] 2. Identify any horizontal asymptotes of the graph of $f(x) = \frac{(3x^2 + 1)^2}{x^3(5 - 6x)}$.

- 3. Consider the function $f(x) = x^2 6x + 9$.
- [7] (a) Use the <u>limit definition</u> of the derivative to find f'(x).

[3] (b) Find the equation of the line that is tangent to the curve $y = x^2 - 6x + 9$ at x = 1.

[13] 4. Consider the function

$$f(x) = \begin{cases} \frac{x+2}{x^2-1}, & \text{for } x < 0\\ 3x+8, & \text{for } x = 0\\ \frac{x^2-4x+4}{x-2}, & \text{for } x > 0 \end{cases}$$

(a) Use the definition of continuity to determine whether f(x) is continuous at x = 0. If it is not, is the discontinuity removable or non-removable?

(b) Use the definition of continuity to determine all other points at which f(x) is not continuous. Classify any discontinuities as removable or non-removable.