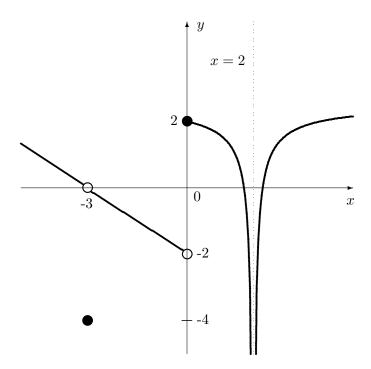
TEST 1

## **MATHEMATICS 1000-005**

October 10th, 2024

Name MUN Number

[12] 1. Use the graph of y = f(x) below to determine each of the following. Label the limits as  $\infty$  or  $-\infty$  where appropriate. If the limit does not exist or the value of the function is undefined, indicate this.



(a) 
$$f(2) =$$

(b) 
$$\lim_{x \to 2^{-}} f(x) =$$

(c) 
$$\lim_{x \to 2^+} f(x) =$$

(d) 
$$\lim_{x \to 2} f(x) =$$

(e) 
$$f(0) =$$

$$(f) \quad \lim_{x \to 0^{-}} f(x) =$$

$$(g) \quad \lim_{x \to 0^+} f(x) =$$

$$(h) \quad \lim_{x \to 0} f(x) =$$

(i) 
$$f(-3) =$$

$$(j) \quad \lim_{x \to -3^{-}} f(x) =$$

$$\text{(k)} \quad \lim_{x \to -3^+} f(x) =$$

$$(\ell) \quad \lim_{x \to -3} f(x) =$$

[16] 2. Determine each of the following limits. If a limit does not exist, explain why.

(a) 
$$\lim_{x \to 2} \frac{3x - 6}{3 - \sqrt{5x - 1}}$$

(b) 
$$\lim_{x \to 0} \frac{\sin^2(5x)}{x^2}$$

(c) 
$$\lim_{x \to -3} \left[ \frac{6}{x^2 - 9} - \frac{1}{x^2 + 5x + 6} \right]$$

[4] 3. Identify any horizontal asymptotes to the graph of  $f(x) = \frac{6x^2 + 7}{x(1 - 3x)}$ .

[8] 4. Given the function

$$f(x) = \begin{cases} kx + 7, & \text{for } x < 3\\ 2\sqrt{k+5}, & \text{for } x = 3\\ x + k^2, & \text{for } x > 3 \end{cases}$$

for some constant k, determine each of the following.

- (a) All values of k for which  $\lim_{x\to 3} f(x)$  exists.
- (b) All values of k for which f(x) is continuous at x = 3.
- (c) All values of k for which f(x) has a removable discontinuity at x = 3.