

Mathematics 2000: Assignment #3, Winter 2004

Due Feb 4

A professor had a file with convergent series and another file with divergent series. Accidentally the files were mixed up. Please, help the professor to sort things out.

1. Usint the integral test.

$$\begin{array}{lll} \text{a) } \sum_{n=1}^{\infty} \frac{1}{n^4} & \text{b) } \sum_{n=1}^{\infty} \frac{1}{n^{1/4}} & \text{c) } \sum_{n=1}^{\infty} \frac{n^2}{n^3 + 1} \\ \text{d) } \sum_{n=2}^{\infty} \frac{1}{n \ln n} & \text{e) } \sum_{n=2}^{\infty} \frac{1}{n(\ln n)^2} & \text{f) } \sum_{n=2}^{\infty} \frac{\ln n}{n^2} \end{array}$$

2 Using the comparison tests

$$\begin{array}{lll} \text{a) } \sum_{n=1}^{\infty} \frac{n^{3/2}}{n^4 + n + 1} & \text{b) } \sum_{n=1}^{\infty} \frac{1}{(n^2 + n + 2)^{1/4}} & \text{c) } \sum_{n=1}^{\infty} \frac{\sqrt{n^2 - n + 7}}{n^3 + n^2 - 125n + 678} \\ \text{d) } \sum_{n=1}^{\infty} \frac{1 + \sin^2 n}{2^n} & \text{e) } \sum_{n=1}^{\infty} \tan\left(\frac{1}{n}\right) & \text{f) } \sum_{n=1}^{\infty} \cot\left(\frac{1}{n^2}\right) \\ \text{g) } \sum_{n=1}^{\infty} \frac{5^n}{3^n + 4} & \text{h) } \sum_{n=1}^{\infty} \frac{3^n}{4^n + 4} & \text{i) } \sum_{n=1}^{\infty} \frac{2^n + 3^{n/2} + 2^{2n}}{4^n} \\ \text{j) } \sum_{n=1}^{\infty} \frac{(n+1)!}{(n+2)!} & \text{k) } \sum_{n=1}^{\infty} \frac{n!}{(n+2)!} & \text{l) } \sum_{n=1}^{\infty} \frac{n}{n!} \end{array}$$

3. Using the alternating series test.

$$\begin{array}{ll} \text{a) } \sum_{n=1}^{\infty} (-1)^n \frac{n^2}{n^3 + 4} & \text{b) } \sum_{n=2}^{\infty} (-1)^n \frac{n}{\ln n} \\ \text{c) } \sum_{n=1}^{\infty} (-1)^n \tan\left(\frac{1}{n}\right) & \text{d) } \sum_{n=1}^{\infty} (-1)^n \cot\left(\frac{1}{n}\right) \\ \text{e) } \sum_{n=3}^{\infty} (-1)^n \frac{1}{\ln n} & \text{f) } \sum_{n=1}^{\infty} (-1)^n \frac{n^n}{n!} \end{array}$$

Bonus problem Are the following series convergent or divergent?

$$\begin{array}{l} \text{a) } \sum_{n=2}^{\infty} \frac{1}{n(\ln n)(\ln \ln n)} \\ \text{b) } \sum_{n=2}^{\infty} \frac{1}{n(\ln n)(\ln \ln n)(\ln \ln \ln n)(\ln \ln \ln \ln n)} \\ \text{c) } \sum_{n=2}^{\infty} \frac{1}{n(\ln n)(\ln \ln n)(\ln \ln \ln n)(\ln \ln \ln \ln n) \dots (\ln \ln \dots \ln n)} \end{array}$$