

Instructions

- Answer each question completely; justify your answers.
 - This assignment is due at: 5:00 pm on Tuesday October 21st.
1. Exercise 6.1.14.
 2. Exercise 6.2.8.
 3. Exercise 6.2.14.
 4. Exercise 6.2.18.
 5. Suppose that Nestlé has contracted with an airline to provide small packages of Smarties that are to be distributed to the airline's passengers while in flight. Each package is to contain 20 individual Smarties, coloured red, blue, green, and yellow. Colours red, green, and yellow each need to be represented at least twice per package, but blue should occur at most 3 times (thereby attempting to design the blue candies to be rare).
 - (a) How many different ways are there to fill each package, subject to these constraints?
 - (b) What fraction of the possible ways to fill each package contain blue Smarties?
 6. For each integer $r \geq 0$, find $[x^r]G(x)$, where $G(x) = \left(\frac{1}{1-x^2}\right)\left(\frac{2}{1-x^3}\right)$.
 7. Let a_r denote the number of ways to express r as a sum of perfect squares of positive integers.
 - (a) Find a generating function for a_r .
 - (b) Determine a_{30} .
 8. Find a generating function for a_r , the number of integer solutions to the equation $e_1 + 3e_2 + 3e_3 + 7e_4 = r$, where $0 \leq e_1$, $0 \leq e_2$, $2 \leq e_3 \leq 8$, and $0 \leq e_4 \leq 20$.
 9. Find a generating function for a_r , the number of partitions of r into 4 parts.
 10. Exercise 6.3.2.
 11. Exercise 6.3.4.
 12. Exercise 6.3.12.