## PMAT 4340 – Combinatorial Analysis Fall 2006

## Instructions

- Answer each question completely; justify your answers.
- This assignment is due at: 5:00 pm on Wednesday November 22nd.
- 1. Solve the following linear recurrence relation:  $a_n = -7a_{n-1} 9a_{n-2}, a_0 = 0, a_1 = 1.$
- 2. Solve the following inhomogeneous recurrence relations:
  - (a)  $a_n = 2a_{n-1} + n, a_0 = 17.$
  - (b)  $a_n = 4a_{n-1} 3^n, a_0 = 1.$
  - (c)  $a_n = 3a_{n-1} 2n + n^2, a_0 = 0.$
- 3. Use generating functions to solve the following recurrence relations:
  - (a)  $a_n = a_{n-1} 3n, a_0 = 3.$
  - (b)  $a_n = 3a_{n-1} + 4a_{n-2}, a_0 = 1, a_1 = 2.$
  - (c)  $a_n = 3a_{n-1} + 2^n, a_0 = 1.$
  - (d)  $a_n = 3a_{n-1} 2a_{n-2} + n, a_0 = 2, a_1 = 4.$
- 4. Exercise 7.5.14.