

**Instructions**

- Answer each question completely; justify your answers.
  - This assignment is due at: 5:00 pm on Wednesday October 25th.
1. Exercise 6.1.16.
  2. Exercise 6.1.20.
  3. Exercise 6.1.24.
  4. Exercise 6.2.10.
  5. Exercise 6.2.14.
  6. Exercise 6.2.16.
  7. Exercise 6.2.22.
  8. Exercise 6.2.26.
  9. Exercise 6.2.34.
  10. Let  $a_r$  denote the number of ways to express  $r$  as a sum of perfect squares of positive integers.
    - (a) Find a generating function for  $a_r$ .
    - (b) Determine  $a_{30}$ .
  11. Find a generating function for  $a_r$ , the number of integer solutions to the equation  $e_1 + 3e_2 + 3e_3 + 7e_4 = r$ , where  $0 \leq e_1$ ,  $0 \leq e_2$ ,  $2 \leq e_3 \leq 8$ , and  $0 \leq e_4 \leq 20$ .
  12. Find a generating function for  $a_r$ , the number of partitions of  $r$  into 4 parts.
  13. Exercise 6.3.2.
  14. Exercise 6.3.4.
  15. Exercise 6.3.12.