## MATH 3370 – Number Theory Fall 2012

## Instructions

- Answer each question completely; justify your answers.
- This assignment is due at 17:00 on Wednesday October 24th in Assignment Box #43.
- 1. Exercise 3.7.
- 2. Exercise 3.8.
- 3. Prove that a number is divisible by 3 if and only if the sum of its digits is divisible by 3.
- 4. Exercise 3.15.
- 5. Exercise 4.5.
- 6. Exercise 4.14.
- 7. Exercise 4.16.
- 8. Exercise 4.21.
- 9. Wilson's theorem asserts that if p is a prime then  $(p-1)! \equiv -1 \pmod{p}$ . Prove the converse of Wilson's theorem.
- 10. Without factoring n, prove that n = 901 is composite.