

$$2. c) \vec{PC} = \begin{bmatrix} -1-3 \\ 0-2 \\ 1-1 \end{bmatrix} = \begin{bmatrix} -4 \\ -2 \\ 0 \end{bmatrix} \quad \underline{n} = \begin{bmatrix} -3 \\ -3 \\ 3 \end{bmatrix}$$

$$\begin{aligned} \underline{p} &= \text{proj}_{\underline{n}} \vec{PC} = \frac{\vec{PC} \cdot \underline{n}}{\underline{n} \cdot \underline{n}} \underline{n} \\ &= \frac{(-4)(-3) + (-2)(-3) + 0(3)}{(-3)^2 + (-3)^2 + 3^2} \begin{bmatrix} -3 \\ -3 \\ 3 \end{bmatrix} \\ &= \frac{18}{27} \begin{bmatrix} -3 \\ -3 \\ 3 \end{bmatrix} \\ &= \frac{2}{3} \begin{bmatrix} -3 \\ -3 \\ 3 \end{bmatrix} \\ &= \begin{bmatrix} -2 \\ -2 \\ 2 \end{bmatrix} \end{aligned}$$

$$\|\underline{p}\| = \sqrt{(-2)^2 + (-2)^2 + 2^2} = \sqrt{12} = \boxed{2\sqrt{3}}$$

Observe that $\underline{p} = \vec{PQ}$ so, if Q is the point (x, y, z) then

$$\begin{bmatrix} x-3 \\ y-2 \\ z-1 \end{bmatrix} = \begin{bmatrix} -2 \\ -2 \\ 2 \end{bmatrix}$$

$$\text{so } x-3 = -2 \rightarrow x = 1$$

$$y-2 = -2 \rightarrow y = 0$$

$$z-1 = 2 \rightarrow z = 3$$

so Q is the point $(1, 0, 3)$.