

REVIEW
SESSION

Dec. 7/09

HYPOTHESIS TESTING

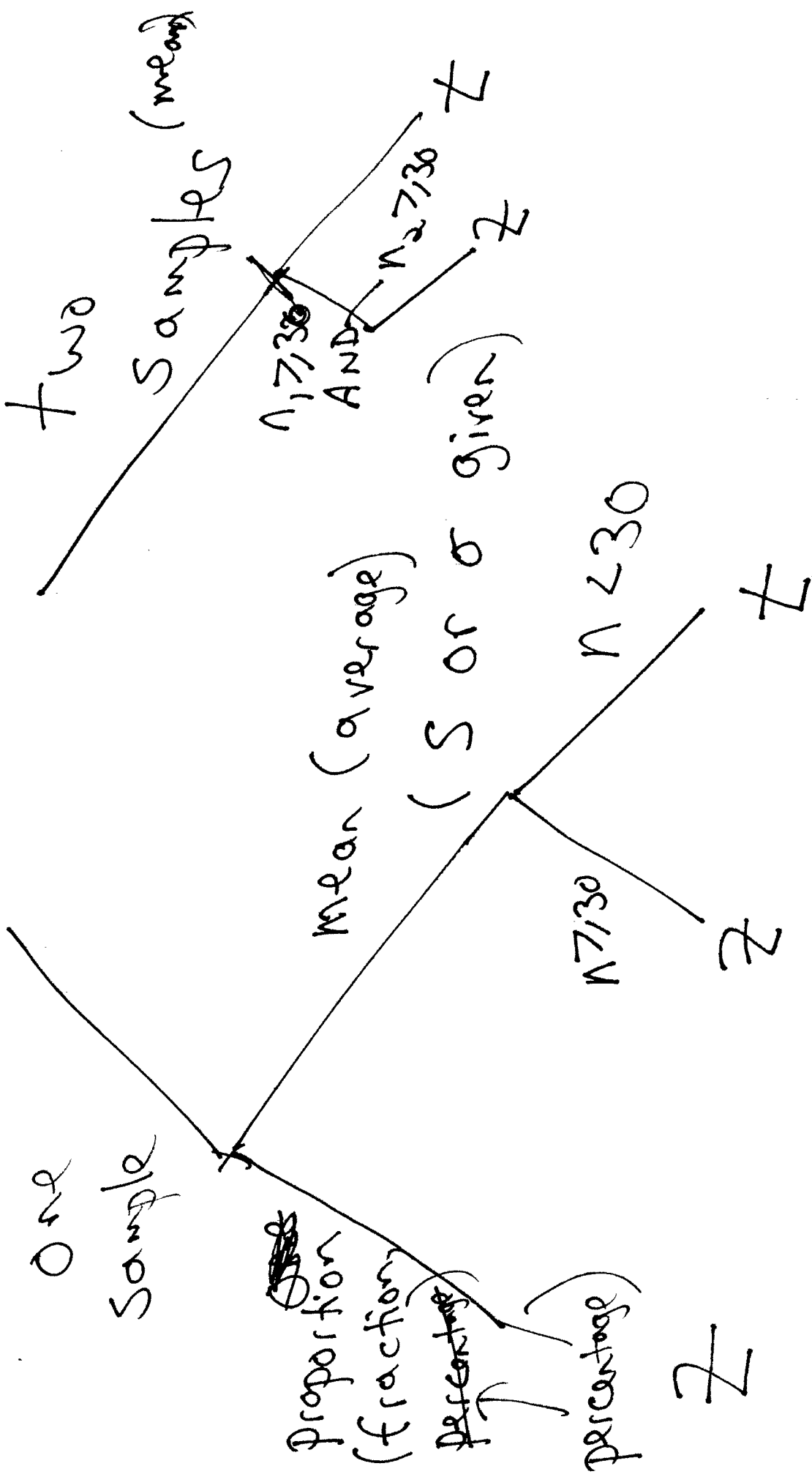
If problem has word 'test' in it,

⇒ do hypothesis testing.

(i.e. H_0 , H_1 , test statistic,

reject or don't reject
 H_0)

Testing



EX: $H_0: \mu = 25$

$H_1: \mu > 25$

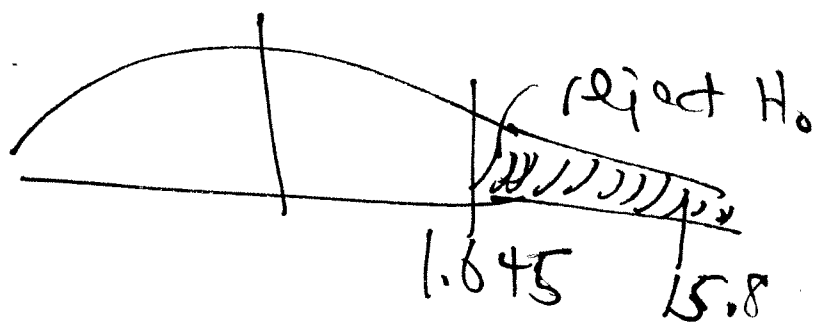
$\bar{x} = 40, \sigma = 6, n = 40.$

$$z = \frac{\bar{x} - \mu}{\sigma / \sqrt{n}} = \frac{40 - 25}{6 / \sqrt{40}} = \boxed{15.8}$$

→ Rejection Region: Reject H_0 if

$$z > z_{\alpha}.$$

Suppose $\alpha = 0.05$ given: $z_{.05} = 1.645$

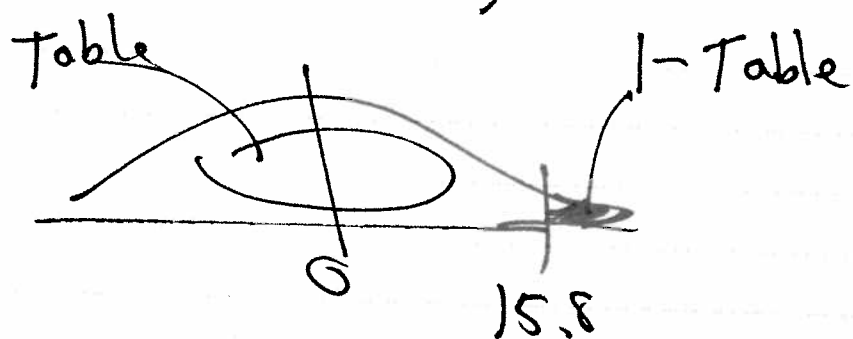


(or 1.64)
or 1.65)

Since $15.8 > 1.645$, reject H_0 .

$$H_1: \mu > 25$$

p-value: $P(Z > 15.8)$



Use 3.70 from table:

$$P(Z > 15.8) \approx 1 - .9999$$
$$= \boxed{0.0001}$$

RULE: If p-value $\leq \alpha$, reject H_0 .

$\alpha = 0.05$: Since $.0001 < .05$,
Reject H_0 .

ONLY NEED To be able to find
p-values for Z , not t .

p. 365, #1

1 sample

EX: 5 cities are randomly selected, and it is found $n < 30$ that average mayor's salary \bar{x} for these cities is \$133,000 with a standard deviation of \$12,000.

Does it appear that the avg. mayor's salary in all cities differs \neq from \$125,000?

No, Test at $\alpha = 0.05$.
 H_0 ,
etc.

$$H_0: \mu = 125000$$

$$H_1: \mu \neq 125000$$

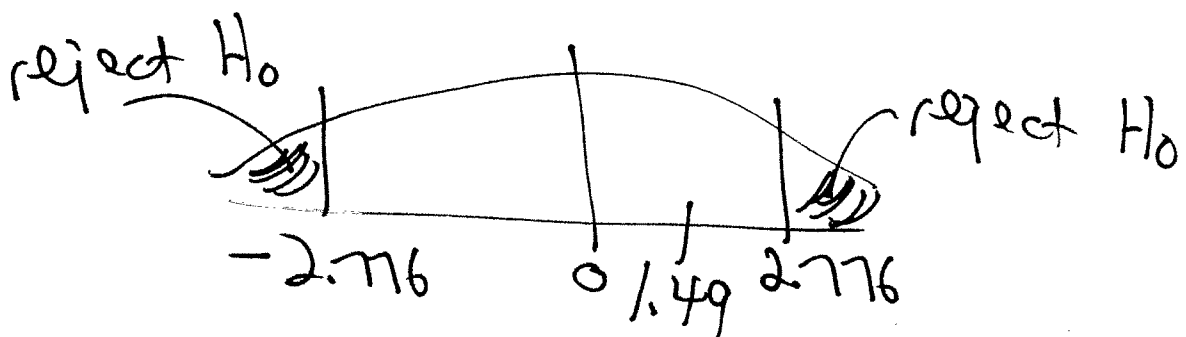
$$t = \frac{\bar{y} - \mu}{s/\sqrt{n}} = \frac{133000 - 125000}{12000/\sqrt{5}} = 1.49$$

$\alpha = 0.05$; reject H_0 if

$$t > t_{\alpha/2} \text{ or } t < -t_{\alpha/2}$$

Using (T-table) with $(n-1) = 4$ df.

$$t_{0.025} = 2.776$$



Since $1.49 < 2.776$, don't reject H_0 .

Avg. Mayor's salary does not differ from \$125000.

one-tail or two-tail?

$$H_1: \mu > 25$$

↑
("greater", "above",
"more than").

$$H_1: \mu \neq 120000$$

("different", "not the same",
"has changed").

$$H_1: p \leq 0.2$$

↑
("smaller", "below",
"less than")

EX: The mean family income in a large city is \$45000.

The incomes are normally distributed and 77% of family incomes are below \$51000.

Find the standard deviation of the distribution.

→ ① Use z-score: $z = \frac{x - \mu}{\sigma}$

② Use table.

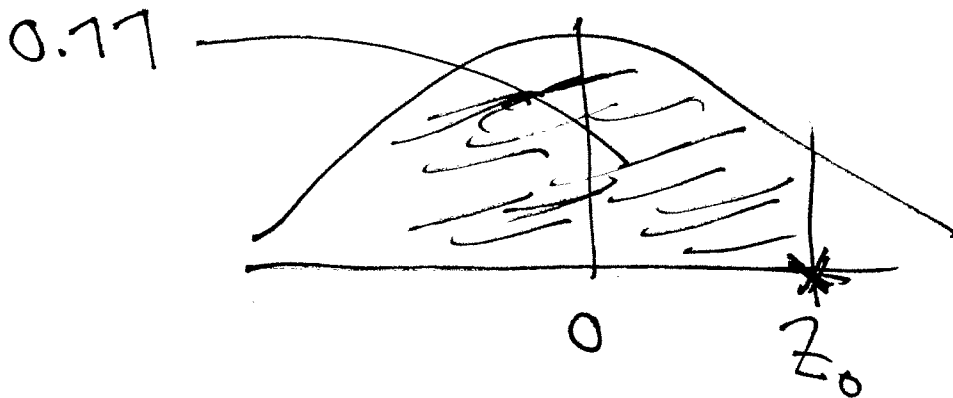
$X = \text{income.}$ $X \sim N(45000, \sigma)$
find this
↓

$$P(X < 51000) = 0.77$$

$$P\left(Z < \frac{51000 - 45000}{\sigma}\right) = 0.77$$

$$= P\left(Z < \frac{6000}{\sigma}\right) = 0.77$$

$$\Rightarrow P\left(Z < \frac{z_0}{\sigma}\right) = 0.77. \text{ Find } z_0.$$



find 0.77 in MIDDLE of table: $z_0 = 0.74$

$$0.74 = \frac{6000}{\sigma}$$

$$\sigma = \frac{6000}{0.74} = 8108$$

(p. 222, #15) (Sect 5-3)

EX: A lottery offers one
\$100 prize, 2 \$50
prizes and 2 \$10 prizes.
200 tickets are sold
at \$2 each. Find
the expected profit from
~~buy~~ buying one ticket.

$$\begin{aligned}\text{profit} &= \text{win} - \text{spend} \\ &= \text{win} - 2 \\ &= \begin{cases} 100 - 2 = 98 \\ 50 - 2 = 48 \\ 10 - 2 = 8 \\ 0 - 2 = -2 \end{cases}\end{aligned}$$

$X = \text{profit}$

X	98	48	8	-2
$p(X)$	$\frac{1}{200}$	$\frac{2}{200}$	$\frac{2}{200}$	$\frac{195}{200}$

$(200 - 5 \text{ winning tickets})$

Expected Profit: $\mu = \sum Xp(X)$

$$= 98\left(\frac{1}{200}\right) + 48\left(\frac{2}{200}\right)$$

$$+ 8\left(\frac{2}{200}\right) - 2\left(\frac{195}{200}\right)$$

$$= \boxed{-0.9}$$

P-166, #17 :

\bar{A}

	Channel 6	Ch. 8	Ch. 10
→ Quiz Comedy	5 ✓	2	1
→ Drama	3	2	8
	4 ✓	4	2

B

A : { show not on ch. 6 }

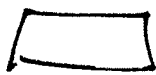

B : { show is Quiz or Drama
and not on ch. 10 }

$P(\bar{A} \text{ and } B) = ?$

Tried: $P(\bar{A} \text{ and } B) = P(\bar{A}) \cdot P(B)$.

Can only do this if question
tells us that \bar{A} and B are
independent (can't assume!)

find $P(\bar{A} \text{ and } B)$ by brute force.

→ need to be in  and 
at same time

$$P(\bar{A} \text{ and } B) = \frac{5 + 4}{5 + 2 + 1 + 3 + 2 + 8 + 4 + 4 + 2}$$
$$=$$

#25, p.179: OMIT.