

1. Is the following vector field irrotational or incompressible at point $(0, 1, 2)$?

$$\vec{F} = \left(\frac{x}{x^2 + y^2 + z^2}, \frac{y}{x^2 + y^2 + z^2}, \frac{z}{x^2 + y^2 + z^2} \right)$$

2. Evaluate the surface integral for given function

(a) $\int \int_{\mathbf{S}} y \, dS$, where \mathbf{S} is a surface $z = 2/3(x^{3/2} + y^{3/2})$, $0 \leq x \leq 1$, $0 \leq y \leq 1$.

(b) $\int \int_{\mathbf{S}} \sqrt{1 + x^2 + y^2} \, dS$, where \mathbf{S} is the helocoid with vector equation $\vec{r}(u, v) = (u \cos v, u \sin v, v)$, $0 \leq u \leq 1$, $0 \leq v \leq \pi$.

3. Evaluate the surface integral for given vector field

(a) $\int \int_{\mathbf{S}} \vec{F} \cdot d\vec{S}$, where $\vec{F}(x, y, z) = (xy, 4x^2, yz)$ and \mathbf{S} is a surface $z = xe^y$, $0 \leq x \leq 1$, $0 \leq y \leq 1$, with upward orientation.

(b) $\int \int_{\mathbf{S}} \vec{F} \cdot d\vec{S}$, where $\vec{F}(x, y, z) = (y, x, z^2)$ and \mathbf{S} is the helocoid with vector equation $\vec{r}(u, v) = (u \cos v, u \sin v, v)$, $0 \leq u \leq 1$, $0 \leq v \leq \pi$, with upward orientation.

4. Use Stokes's Theorem to evaluate surface integral $\int \int_{\mathbf{S}} \text{curl} \vec{F} \cdot d\vec{S}$, where $\vec{F}(x, y, z) = (yz, xz, xy)$, and surface \mathbf{S} is a part of paraboloid $z = 9 - x^2 - y^2$ that lies above the plane $z = 5$, oriented upward.

5. Use Stokes's Theorem to evaluate line integral $\int_C \vec{F} \cdot d\vec{r}$, where $\vec{F} = (e^{-x}, e^x, e^z)$, and C is the boundary of the plane $2x + y + 2z = 2$ in the first octant, oriented counterclockwise as viewed from above.

6. Verify that Divergence theorem is true for the vector field $\vec{F} = (x^2, xy, z)$ and the solid bounded by paraboloid $z = 4 - x^2 - y^2$ and xy -plane.

7. Verify that Divergence theorem is true for the vector field $\vec{F} = (x, y, z)$ and the unit ball $x^2 + y^2 + z^2 = 1$.