## Due Tue Jan 18

1. Given parametric equations find equation in the form F(x, y) = 0 and sketch the curve. Do you know its name?

(a) 
$$x = \sec t, y = \tan t, -\pi/2 < t < \pi/2$$
  
(b)  $x = e^t, y = 1 - e^{-t}, -\ln 2 \le t \le \ln 2$   
(c)  $x = 2\cos t, y = 3\sin t, -\pi < t < \pi$   
(d)  $x = 2\cos(2t), y = 2\sin(2t), -\pi/2 < t < \pi/2$ 

- 2. For each curve from the previous problem find and sketch tangent vector at t = 0.
- 3. Sketch 3D curve and find tangent vector at each time t.

(a) 
$$x = \cos(2t), y = 1, z = 2, -\pi/2 < t < \pi/2$$
  
(b)  $x = \cos(2t), y = 3, z = \sin(2t), -\pi/2 < t < \pi/2$   
(c)  $x = \cos(2t), y = t, z = \sin(2t), -\pi/2 < t < \pi/2$ 

- 4. Find parametric equations for the sides of the triangle with vertices at points (1, 2, 3), (-1, 5, 6), (0, 5, 1).
- 5. Find parametric equations for the curve of intersection of cylinder  $x^2 + y^2 = 4$  and z = xy. Can you imagine and sketch the curve? Please!
- 6. Find vector position vector  $\vec{r}(t)$  if the velocity vector is given by

(a) 
$$\frac{4}{1+t^2}\mathbf{i} + \frac{2t}{1+t^2}\mathbf{j} + \frac{t^2}{1+t^2}\mathbf{k}$$

(b)  $e^{2t}\mathbf{i} + \ln t\mathbf{j} + \sec^2 t\mathbf{k}$