MEMORIAL UNIVERSITY OF NEWFOUNDLAND DEPARTMENT OF MATHEMATICS AND STATISTICS

- 1. For each of the following matrices find:
 - 1. the matrix of cofactors;
 - 2. the determinant using the cofactor (Laplace) expansion;
 - 3. the inverse matrix using the cofactors;

$$A = \begin{bmatrix} 2a & a^2 \\ a^3 & a^4 \end{bmatrix}, \qquad B = \begin{bmatrix} 3 & -5 & 1 \\ 5 & -10 & 5 \\ 2 & 0 & -1 \end{bmatrix}, \qquad C = \begin{bmatrix} 1 & 0 & 0 & a \\ 0 & 1 & b & 0 \\ 0 & c & 1 & 0 \\ d & 0 & 0 & 1 \end{bmatrix}.$$

2. Find the determinant by rewriting the matrix in a triangular form

$$C = \begin{bmatrix} 1 & 2 & 3 & 4 & 5 \\ 2 & 6 & 9 & 12 & 15 \\ 1 & 2 & 6 & 8 & 10 \\ 1 & 2 & 3 & 8 & 10 \\ 2 & 4 & 6 & 12 & 20 \end{bmatrix}.$$

- 3. Find conditions for a and b such that the matrix $\begin{bmatrix} 8 & a^2 & a \\ b & 7 & a \\ 0 & a 2b & 0 \end{bmatrix}$ is invertable?
- 4. Let det A = 3, det B = 4, and det C = 5; and let A and B be 3×3 matrices , and C be 4×4 . Find: det $(A^T B^2 A^3 B^{-1})$; det $(2A^2) - det(2B) + det(2C)$; det(ABC).
- 5. True of False? Explain.
 - a) If a matrix is symmetric $(A^T = A)$ then it is invertable.
 - b) If matrix is diagonal then it is invertable.
 - c) Elementary row operations always change the determinant of the matrix.
 - d) If A and B are invertable matrices then $((AB)^{-1})^T = (A^T)^{-1}(B^T)^{-1}$.