PMAT 4340 – Combinatorial Analysis Fall 2008

Instructions

- Answer each question completely; justify your answers.
- This assignment is due at: 5:00 pm on Wednesday November 12th.
- 1. How many *r*-digit quaternary sequences are there in which the total number of 0's and 1's is odd?
- 2. Exercise 6.4.14.
- 3. Find an ordinary generating function $g(x) = \sum_{r \ge 0} a_r x^r$ such that
 - (a) $a_r = 5r^2$
 - (b) $a_r = 8 3r$
 - (c) $a_r = r(r-1)(r-2)\cdots(r-27)$
- 4. Find an ordinary generating function $g(x) = \sum_{r \ge 0} a_r x^r$ such that
 - (a) $a_r = r^2 \frac{3r}{7}$ (b) $a_r = (r+2)(r+1)(r) \cdots (r-66)$
- 5. Exercise 6.5.2.
- 6. Exercise 6.5.6.

7. Evaluate
$$\sum_{i=0}^{n} i^{3}$$
.
8. Evaluate $\sum_{i=0}^{n} \left(4 - i(i+1)(i+2)\right)$

- 9. Exercise 7.1.6.
- 10. Exercise 7.1.12.
- 11. Exercise 7.1.20.