${ m PMAT}$ 4340 — Combinatorial Analysis Fall 2006

Assignment #6

Instructions

- Answer each question completely; justify your answers.
- This assignment is due at: 5:00 pm on Wednesday November 1st.
- 1. Exercise 6.3.15.
- 2. Exercise 6.3.17.
- 3. Exercise 6.4.2.
- 4. Exercise 6.4.6.
- 5. Exercise 6.4.8.
- 6. How many r-digit quaternary sequences are there in which the total number of 0's and 1's is odd?
- 7. Exercise 6.4.12.
- 8. Find an ordinary generating function $g(x) = \sum_{r>0} a_r x^r$ such that
 - (a) $a_r = 7r^2$
 - (b) $a_r = 5 3r$
 - (c) $a_r = r(r-1)(r-2)\cdots(r-17)$
- 9. Find an ordinary generating function $g(x) = \sum_{r \geq 0} a_r x^r$ such that
 - (a) $a_r = 5r^2 \frac{3r}{2}$
 - (b) $a_r = (r+2)(r+1)(r) \cdots (r-99)$
- 10. Exercise 6.5.2.
- 11. Exercise 6.5.6.
- 12. Evaluate $\sum_{i=0}^{n} i^3$.
- 13. Evaluate $\sum_{i=0}^{n} 4 i(i+1)(i+2)$.
- 14. Exercise 7.1.4.
- 15. Exercise 7.1.6.