

**Instructions**

- Answer each question completely; justify your answers.
  - This assignment is due at 17:00 on Thursday November 10th in Assignment Box #23.
1. Let  $a = 81876$  and  $b = 1198$ . Let  $g$  be the greatest common divisor of  $a$  and  $b$ .
    - (a) Find  $g$ .
    - (b) Find integers  $m$  and  $n$  such that  $ma + nb = g$ .
    - (c) What is the least common multiple of  $a$  and  $b$ ?
  2. Find integers  $x$  and  $y$  such that  $154x + 260y = 4$ .
  3. Show that there is no integral solution to  $196x + 260y = 3$ .
  4. Prove: if  $k \in \mathbb{N}$  then  $\gcd(3k + 2, 5k + 3) = 1$ .
  5. Find the prime decompositions for:
    - (a)  $n = 123456$
    - (b)  $n = 5000$
  6. Exercise 4.3.9.
  7. Exercise 4.3.26, part (b).
  8. Exercise 4.3.32, parts (b) and (c).
  9. Exercise 4.3.35.