

**Instructions**

- Answer each question completely; justify your answers.
  - This assignment is due at 15:00 on Friday January 25th in Assignment Box #48.
1. Find a BIBD(9, 3, 1).
  2. Suppose that a BIBD has  $v = 8$  and  $k = 4$ . Prove that  $b \geq 14$ .
  3. Prove that no BIBD(10, 8, 4, 5, 2) can exist.
  4. Does the BIBD(7, 7, 3, 3, 1) have an SDR?
  5. How many SDRs are there for the design with these blocks: 123, 234, 345, 451, 512 ?
  6. Suppose that the design  $\mathcal{D}$  has an SDR and suppose that each block of  $\mathcal{D}$  has at least  $t$  elements. Prove that if  $t \leq b$  then  $\mathcal{D}$  has at least  $t!$  SDRs.